

Precalculus-G11-Ch3-Test

Indicate the answer choice that best completes the statement or answers the question.

Evaluate each expression.

1. $\log 75$ B

- a. 7.5 b. 1.88
c. 0.53 d. 3.76

2. Solve $\log_6 x = 2$ A

- a. 36 b. 12
c. 6 d. 64

3. Find $\ln 375$. Round your answer to four decimal places. C

- a. -5.9269 b. 6.9269
c. 5.9269 d. -6.9269

4. Find the amount of time required to double an amount at 5.84% if the interest is compounded continuously. C

- a. 5.15 years b. 5.94 years
c. 11.87 years d. 23.74 years

Express each logarithm in terms of $\ln 3$ and $\ln 5$.

5. $\ln \frac{81}{125}$ C

- a. $4 \ln 5 - 3 \ln 3$ b. $5 \ln 3 - 3 \ln 4$
c. $4 \ln 3 - 3 \ln 5$ d. $3 \ln 4 - 5 \ln 3$

Evaluate each expression.

6. $6^{\log_6 1.5}$ D

- a. 6 b. $6^{1.5}$
c. 1.5^6 d. 1.5

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7. Evaluate the expression $\log_5 \frac{1}{25}$. B

- a. $-\frac{1}{2}$ b. -2
c. $\frac{1}{2}$ d. 2

Evaluate each expression.

8. $\log_3 243$ A

- a. 5 b. 7
c. 4 d. 6

Use the graph of f to describe the transformation that results in the graph of g . Then sketch the graphs of g and f .

9. $f(x) = e^x$; $g(x) = -5e^{x+4} + 2$ C

- a. $g(x)$ is the graph of $f(x)$ translated 4 unit(s) to the **left**, 2 unit(s) **down**, and **expanded** vertically by a factor of **5**.
b. $g(x)$ is the graph of $f(x)$ translated 4 unit(s) to the **left**, 2 unit(s) **up**, and **expanded** vertically by a factor of **5**.
c. $g(x)$ is the graph of $f(x)$ translated 4 unit(s) to the **right**, 2 unit(s) **up**, and **expanded** vertically by a factor of **5**.
d. $g(x)$ is the graph of $f(x)$ translated 4 unit(s) to the **right**, 2 unit(s) **down**, and **expanded** vertically by a factor of **5**.

10. Jimmy invests \$500 in an account with a 3% interest rate, making no other deposits or withdrawals. What will Jimmy's account balance be after 10 years if the interest is compounded 2 times each year? D

- a. \$173.43 b. \$580.27
c. \$903.06 d. \$673.43

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11. Uranium ore is composed of two main isotopes, mostly U_{238} with just a trace amount of U_{235} . The two isotopes cannot be separated using chemical reactions because they are chemically identical. In a sample of Uranium ore 99.85% of the atoms are U_{238} atoms and 0.15% are U_{235} atoms. However, before the Uranium can be used in a nuclear power plant, the proportion of U_{235} must be increased to 15% (thus reducing the proportion of U_{238} to 85%).B

This is done by a process called gas diffusion. The ratio of the masses of these two isotopes is $\frac{238}{235} = 1.013$, which means gaseous U_{238} atoms will travel more slowly than the U_{235} atoms after the uranium ore is vaporized. Each cycle of the gas diffusion process will decrease the U_{238} proportion by 1.3%.

What will the U_{238} percent be after 6 cycles of the gas diffusion process? How many cycles will be needed to reduce the U_{238} percent to 85%?

- a. 86.85%; 7 gas diffusion cycles b. 92.31%; 13 gas diffusion cycles
c. 92.55%; 12 gas diffusion cycles d. 92.05%; 11 gas diffusion cycles

Solve each equation.

12. $4^x + 7 = 5x - 3$ B

- a. -65.13 b. 65.13
c. 14.53 d. 192.7

13. As automobiles age, the average miles traveled per gallon decreases. Determine the regression equation that best models the data.D

Age (years)	MPG
1	35
3	34
5	33
7	31
9	28
11	26
13	23
15	18

- a. power b. logarithmic
c. quadratic d. exponential

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Use the graph of f to describe the transformation that results in the graph of g . Then sketch the graphs of g and f .

14. $f(x) = \left(\frac{1}{2}\right)^x$; $g(x) = \left(\frac{1}{2}\right)^{x+1} - 3$
B

- a. $g(x)$ is the graph of $f(x)$ translated 3 unit(s) to the **left** and 1 unit(s) **down**.
- b. $g(x)$ is the graph of $f(x)$ translated 1 unit(s) to the **right** and 3 unit(s) **down**.
- c. $g(x)$ is the graph of $f(x)$ translated 3 unit(s) to the **right** and 1 unit(s) **down**.
- d. $g(x)$ is the graph of $f(x)$ translated 1 unit(s) to the **left** and 3 unit(s) **down**.

15. Among various populations of plants or animals, diseases spread exponentially. Use the function $y = 8000(1 - e^{-0.03t})$ to model the spread of Common Corn Rust through a field of 8000 corn plants, with t equal to the number of days since the first case of the disease. How many plants will be infected with Common Corn Rust after 10 days?D

- a. 761 b. 236
- c. 5927 d. 2073

16. Use Newton's Law of Cooling, $y = ae^{-kt} + c$, to find the temperature of a substance as a function the time t in minutes that it has spent cooling off. Two samples of the substance were heated in a container of boiling water until their initial temperatures were both 100°C . The first sample will be cooled by being left out at a room temperature of 24°C , and the second sample of the substance will instead be cooled off in a refrigerator with an inside temperature of $c = 4^\circ\text{C}$. The value of a will equal the *difference* between each sample's initial temperature and that sample's surrounding temperature, and the cooling constant of the substance is $k = 0.12$.

C

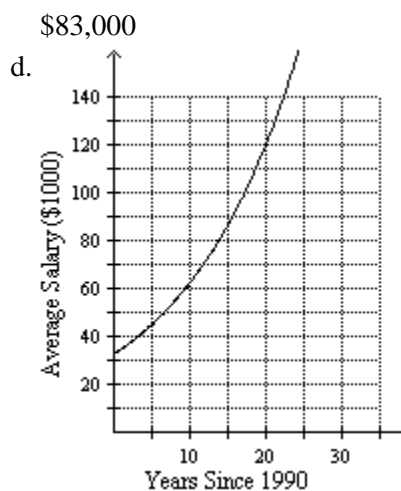
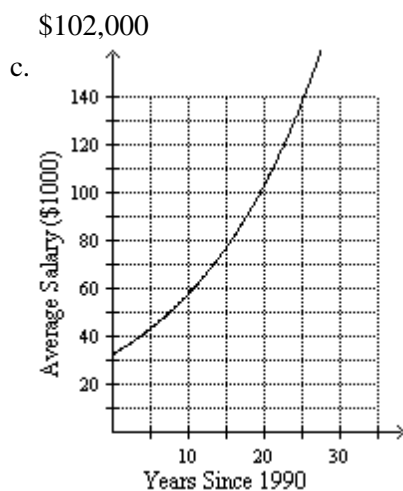
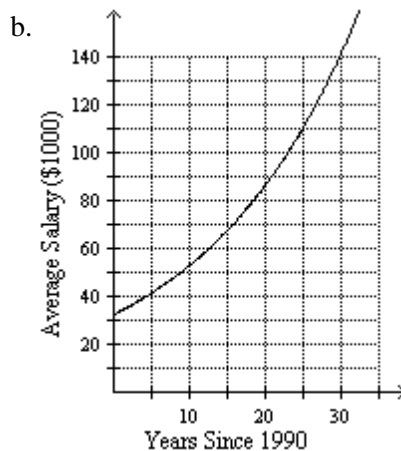
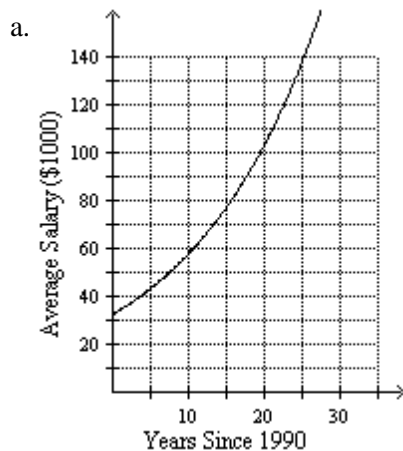
Find the first sample's temperature after it has cooled for 20 minutes. Then find the second sample's temperature after it has cooled for 10 minutes.

- a. 11.1°C ; 30.1°C b. 33.1°C ; 34.1°C
- c. 30.9°C ; 32.9°C d. 26.2°C ; 5.2°C

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17. The nationwide average salary of a computer programmer can be modeled by the equation $y = 31.8 \times (1.06)^n$, where y is the salary in thousands of dollars and n is the number of years since 1990.A

Graph the function. Then, using this model, predict the average programmer's salary in 2010.



\$102,000

\$83,000

\$86,000

\$121,000

Use the graph of f to describe the transformation that results in the graph of g .

18. $f(x) = \log x$; $g(x) = 2\log x + 6A$

- The graph of $g(x)$ is the graph of $f(x)$ expanded vertically by a factor of 2, and translated 6 unit(s) up.
- The graph of $g(x)$ is the graph of $f(x)$ reflected in the x -axis, expanded vertically by a factor of 2, and translated 6 unit(s) up.
- The graph of $g(x)$ is the graph of $f(x)$ expanded vertically by a factor of 2, and translated 6 unit(s) down.
- The graph of $g(x)$ is the graph of $f(x)$ reflected in the x -axis, expanded vertically by a factor of 2, and translated 6 unit(s) down.

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Use the graph of f to describe the transformation that results in the graph of g . Then sketch the graphs of g and f .

19. Find a logarithmic function to model the data.C

x	y
1	60
2	54
3	51
4	50
5	46
6	45
7	44

- a. $f(x) = 60.73(0.95)^x$ b. $f(x) = 0.93(60.73)^x$
 c. $f(x) = 60.04 - 8.25 \ln x$ d. $f(x) = 8.25 - 60.04 \ln x$

Use the graph of f to describe the transformation that results in the graph of g . Then sketch the graphs of g and f .

20. $f(x) = \left(\frac{1}{3}\right)^x$; $g(x) = \left(\frac{1}{3}\right)^{x-2} - 4$
 C

- a. $g(x)$ is the graph of $f(x)$ translated 4 unit(s) to the ~~right~~ and 2 unit(s) down.
 b. $g(x)$ is the graph of $f(x)$ translated 2 unit(s) to the ~~right~~ and 4 unit(s) down.
 c. $g(x)$ is the graph of $f(x)$ translated 2 unit(s) to the ~~left~~ and 4 unit(s) down.
 d. $g(x)$ is the graph of $f(x)$ translated 4 unit(s) to the ~~left~~ and 2 unit(s) down.

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